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## WEAK CONVERGENCE UNDER MAPPING

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Abstract: For a given random element X of a metric space S and a measurable mapping h of S into a metric space  $S_1$  such that  $P\{X \in D_h\} > 0$  we give the conditions for a sequence of random elements  $X_n, n \geq 1$ , of the space S under which the convergence  $X_n \stackrel{D}{\longrightarrow} X$  implies  $h(X_n) \stackrel{D}{\longrightarrow} h(X)$  (Lemma 1) and stronger conditions for  $\{X_n\}$  under which the convergence  $X_n \stackrel{D}{\longrightarrow} X$  implies  $(X_n, h(X_n)) \stackrel{D}{\longrightarrow} (X, h(X))$  (Theorem 3). Here  $D_h$  is the set of discontinuities of h. The case  $S = D[0, \infty)$ ,  $h(x) = \sup_{0 \leq t \leq \infty} x(t)$  is considered in detail.

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