

ON THE CENTRAL LIMIT THEOREM FOR INDEPENDENT RANDOM  
VARIABLES WITH ALMOST SURE CONVERGENCE

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*Abstract:* We obtain an almost sure convergence limit theorem for independent nonidentically distributed random variables. Let  $S_n$ ,  $n \geq 1$ , be the partial sums of independent random variables with zero means and finite variances and let  $a(x)$  be a real function. We present sufficient conditions under which in logarithmic means  $a(S_n/(ES_n^2)^{1/2})$  converges almost surely to  $\int_{-\infty}^{\infty} a(x)d\Phi(x)$ .

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**Key words and phrases:** -

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