

**A Collection of
Numerical Solutions of
Multigrade Equations
Related to the
Prouhet-Tarry-Escott
Problem**

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Notes

I am interested only in solutions leading to symmetric PTE solutions, hence I require a multigrade to be satisfied by all exponents of the same parity up to a certain level.

Pure product solution comes from multiplying polynomials of the form

$$x^p - x^{-p}$$

and then extracting solutions in the well known way.

For even powers there is the same number of terms on both sides (I do not discard zero terms).

For odd powers numbers of left and right terms may differ.

Solution code is composed from:

the largest power

total number of terms

the largest term

the second, third ... largest terms of any side (if needed)

The best results known to me at the moment

Max exponent	Number of terms	Ideal	Known/Ideal
8	10	10	1.000
9	12	11	1.091
10	12	12	1.000
11	20	13	1.538
12	28	14	2.000
13	26	15	1.733
14	30	16	1.875
15	34	17	2.000
16	42	18	2.333
17	48	19	2.526
18	58	20	2.900
19	65	21	3.095
20	70	22	3.182
21	78	23	3.391
22	92	24	3.833
23	94	25	3.760
24	114	26	4.385
25	138	27	5.111
26	160	28	5.714
27	174	29	6.000
28	196	30	6.533
29	207	31	6.677
30	228	32	7.125

Solution code: **8.10.313**

Powers: 2, 4, 6, 8.

Number of terms: **10**

Number of left terms: **5**

Number of right terms: **5**

Left terms:

313, 301, 188, 100, 99

Right terms:

308, 307, 180, 131, 71

Remarks:

Discovered by Peter Borwein, Petr Lisonek and Colin Percival (2002).

Solution code: **8.10.515**

Powers: 2, 4, 6, 8.

Number of terms: **10**

Number of left terms: **5**

Number of right terms: **5**

Left terms:

515, 452, 366, 189, 103

Right terms:

508, 471, 331, 245, 18

Remarks:

Discovered by Peter Borwein, Petr Lisonek and Colin Percival (2002).

Used by Jarosław Wróblewski (November 27, 2009) to produce solution **9.12.1293**.

Solution code: **8.10.23750**

Powers: 2, 4, 6, 8.

Number of terms: **10**

Number of left terms: **5**

Number of right terms: **5**

Left terms:

23750, 20667, 20449, 11857, 436

Right terms:

23738, 20885, 20231, 11881, 12

Remarks:

The smallest member of family of solutions discovered by A. Letac in 1940's.

Solution code	Right terms	Left terms
8.12.36	36, 31, 30, 17, 7, 1	35, 34, 27, 19, 4, 3
8.12.62	62, 54, 47, 35, 27, 9	61, 57, 42, 37, 30, 1
8.12.66	66, 59, 57, 55, 28, 16	64, 62, 60, 49, 33, 11
8.12.71	71, 63, 50, 23, 18, 9	69, 67, 42, 37, 6, 5
8.12.74	74, 67, 47, 46, 27, 15	73, 69, 45, 41, 38, 2
8.12.109	109, 97, 91, 88, 54, 30	107, 99, 98, 74, 65, 24
8.12.111	111, 86, 81, 28, 25, 22	110, 94, 63, 57, 4, 1
8.12.113	113, 97, 89, 52, 31, 10	109, 107, 74, 67, 20, 13
8.12.114	114, 97, 89, 70, 43, 24	111, 106, 75, 73, 56, 2
8.12.119.115	119, 97, 94, 92, 45, 30	115, 111, 90, 74, 68, 7
8.12.119.118	119, 94, 85, 43, 38, 37	118, 101, 67, 61, 50, 7
8.12.137	137, 120, 110, 73, 57, 3	135, 127, 97, 88, 45, 18
8.12.139	139, 124, 115, 89, 42, 18	135, 133, 106, 93, 46, 4
8.12.151	151, 139, 117, 58, 55, 28	149, 143, 113, 70, 37, 36
8.12.158	158, 137, 126, 125, 76, 55	154, 148, 127, 106, 95, 45
8.12.163	163, 145, 138, 103, 56, 14	161, 152, 131, 105, 58, 2
8.12.167	167, 150, 122, 89, 71, 47	163, 158, 109, 93, 85, 34
8.12.179.172	179, 151, 150, 108, 67, 38	172, 171, 123, 122, 74, 25
8.12.179.173	179, 149, 139, 65, 63, 57	173, 167, 111, 91, 81, 5
8.12.179.178	179, 142, 132, 83, 59, 35	178, 151, 111, 103, 55, 28
8.12.195	195, 169, 148, 98, 71, 42	190, 182, 127, 111, 84, 13
8.12.211	211, 165, 155, 59, 54, 44	209, 180, 121, 111, 31, 10
8.12.212	212, 189, 167, 114, 83, 10	206, 202, 148, 133, 75, 9
8.12.222	222, 182, 164, 59, 55, 41	220, 193, 146, 97, 26, 21
8.12.229	229, 215, 166, 118, 63, 48	224, 222, 162, 113, 89, 5
8.12.237	237, 206, 195, 88, 49, 41	231, 223, 179, 104, 50, 3
8.12.243	243, 219, 178, 112, 71, 50	240, 226, 167, 126, 67, 43
8.12.245	245, 213, 202, 141, 101, 22	239, 231, 178, 158, 97, 15
8.12.265.256	265, 240, 204, 179, 73, 67	256, 255, 197, 172, 111, 5
8.12.265.257	265, 229, 223, 133, 72, 4	257, 252, 200, 149, 43, 41
8.12.265.264	265, 229, 219, 108, 88, 6	264, 236, 211, 122, 57, 45
8.12.267	267, 245, 177, 104, 79, 4	265, 249, 168, 124, 61, 13
8.12.282.277	282, 237, 223, 122, 107, 53	277, 257, 197, 138, 118, 3
8.12.282.278	282, 229, 215, 107, 54, 47	278, 250, 177, 149, 37, 9
8.12.295	295, 216, 203, 106, 91, 78	294, 232, 169, 126, 125, 13

Remarks:

Powers: 2, 4, 6, 8 with $6+6=12$ terms.

Results of a selective search by Jarosław Wróblewski (December 2009).

Solution code	Right terms	Left terms
8.12.303	303, 265, 227, 119, 81, 19	291, 289, 191, 167, 45, 7
8.12.325	325, 277, 271, 201, 131, 57	317, 305, 233, 219, 139, 39
8.12.326	326, 273, 243, 227, 112, 89	317, 301, 208, 207, 186, 7
8.12.347	347, 289, 246, 112, 97, 54	343, 306, 194, 192, 43, 41
8.12.358	358, 329, 323, 281, 75, 12	357, 335, 317, 282, 76, 1
8.12.362	362, 295, 291, 163, 118, 81	353, 333, 233, 205, 134, 6
8.12.365	365, 305, 291, 219, 139, 79	355, 339, 241, 229, 181, 15
8.12.370	370, 311, 252, 201, 101, 61	369, 316, 241, 205, 123, 14
8.12.375	375, 325, 266, 184, 162, 61	371, 338, 230, 215, 171, 24
8.12.392	392, 328, 308, 241, 125, 109	385, 356, 277, 224, 197, 32
8.12.405	405, 362, 351, 205, 162, 49	393, 390, 331, 210, 167, 29
8.12.407.398	407, 363, 328, 265, 98, 70	398, 385, 293, 287, 120, 22
8.12.407.405	407, 386, 249, 129, 105, 2	405, 389, 243, 154, 74, 27
8.12.412	412, 358, 337, 161, 154, 27	407, 378, 314, 203, 92, 71
8.12.418	418, 368, 335, 237, 149, 66	402, 401, 302, 253, 165, 16
8.12.421	421, 357, 343, 274, 76, 62	419, 372, 323, 281, 98, 14
8.12.438	438, 389, 335, 256, 122, 97	430, 409, 302, 277, 151, 48

Remarks:

Powers: 2, 4, 6, 8 with $6+6=12$ terms.

Results of a selective search by Jarosław Wróblewski (December 2009).

Solution code: **8.12.541****Powers: 2, 4, 6, 8.**Number of terms: **12**Number of left terms: **6**Number of right terms: **6****Left terms:**

541, 503, 339, 176, 140, 73

Right terms:

532, 517, 305, 251, 96, 31

Remarks:

A member of family of solutions discovered by Jarosław Wróblewski (November 2009).

Left side terms:

$$2 a + 5 b + d$$

$$2 a + 5 b - d$$

$$5 a - 2 b + c$$

$$5 a - 2 b - c$$

$$4 a + 6 b$$

$$6 a - 4 b$$

Right side terms:

$$5 a + 2 b + c$$

$$5 a + 2 b - c$$

$$-2 a + 5 b + d$$

$$-2 a + 5 b - d$$

$$6 a + 4 b$$

$$-4 a + 6 b$$

Assume:

$$c^2 = p * a^2 + q * b^2$$

$$d^2 = p * b^2 + q * a^2$$

$$p = -11/5$$

$$q = 64/5$$

This solution is obtained with

$$a = 118$$

$$b = 89$$

$$c = 266$$

$$d = 401$$

Solution code: **8.12.55292**

Powers: 2, 4, 6, 8.

Number of terms: **12**

Number of left terms: **6**

Number of right terms: **6**

Left terms:

55292, 50841, 50712, 41050, 23681, 11369

Right terms:

54280, 54151, 45759, 44489, 20902, 14148

Remarks:

A member of family of solutions discovered by Jarosław Wróblewski (November 2009).

Left side terms:

$a + 10 b + d$

$a + 10 b - d$

$10 a - b + c$

$10 a - b - c$

$a + 11 b$

$11 a - b$

Right side terms:

$10 a + b + c$

$10 a + b - c$

$-a + 10 b + d$

$-a + 10 b - d$

$11 a + b$

$-a + 11 b$

Assume:

$$c^2 = p * a^2 + q * b^2$$

$$d^2 = p * b^2 + q * a^2$$

$$p = -27/5$$

$$q = 248/5$$

This solution is obtained with

$a = 9533$

$b = 3439$

$c = 9791$

$d = 66661$

Solution code: **9.12.323**

Powers: 1, 3, 5, 7, 9.

Number of terms: **12**

Number of left terms: **6**

Number of right terms: **6**

Left terms:

323, 289, 269, 173, 91, 7

Right terms:

313, 311, 247, 193, 59, 29

Remarks:

Discovered by Chen Shuwen (2000).

Solution code: **9.12.407**

Powers: 1, 3, 5, 7, 9.

Number of terms: **12**

Number of left terms: **6**

Number of right terms: **6**

Left terms:

407, 347, 341, 181, 163, 23

Right terms:

403, 371, 311, 221, 119, 37

Remarks:

Discovered by Jarosław Wróblewski (November 28, 2009).

Solution code: **9.12.463**

Powers: 1, 3, 5, 7, 9.

Number of terms: **12**

Number of left terms: **6**

Number of right terms: **6**

Left terms:

463, 391, 335, 217, 161, 43

Right terms:

461, 403, 287, 283, 91, 85

Remarks:

Discovered by Jarosław Wróblewski (November 28, 2009).

Solution code: **9.12.1293**

Powers: 1, 3, 5, 7, 9.

Number of terms: **12**

Number of left terms: **6**

Number of right terms: **6**

Left terms:

1293, 1167, 995, 679, 399, 57

Right terms:

1279, 1205, 925, 767, 299, 115

Remarks:

Constructed by Jarosław Wróblewski (November 27, 2009) from solution **8.10.515**.

Solution code: **10.12.151**

Powers: 2, 4, 6, 8, 10.

Number of terms: **12**

Number of left terms: **6**

Number of right terms: **6**

Left terms:

151, 140, 127, 86, 61, 22

Right terms:

148, 146, 121, 94, 47, 35

Remarks:

Discovered by Nuutti Kuosa (1999) using a computer program written by Jean-Charles Meyrignac, as a single-grade solution to power 10. Four days later Chen Shuwen noticed it was in fact a multigrade.

Solution code: **10.12.1511**

Powers: 2, 4, 6, 8, 10.

Number of terms: **12**

Number of left terms: **6**

Number of right terms: **6**

Left terms:

1511, 1138, 1075, 700, 622, 107

Right terms:

1510, 1180, 953, 886, 413, 293

Remarks:

The smallest solution of the infinite family of solutions constructed in:

Ajai Choudhry, Jarosław Wróblewski, *Ideal Solutions of the Tarry-Escott Problem of degree eleven with applications to Sums of Thirteenth Powers*, Hardy-Ramanujan Journal, Vol. 31 (2008) pp. 1-13

Solution code: **10.12.2058**

Powers: 2, 4, 6, 8, 10.

Number of terms: **12**

Number of left terms: **6**

Number of right terms: **6**

Left terms:

2058, 1896, 1618, 1109, 891, 257

Right terms:

2037, 1947, 1514, 1294, 639, 472

Remarks:

Discovered by David Broadhurst (2007):

D. Broadhurst, *A Chinese Prouhet-Tarry-Escott solution*,

<http://physics.open.ac.uk/~dbroadhu/cpte.pdf>

The second known solution.

It was later used by Ajai Choudhry and Jarosław Wróblewski to produce an infinite family of solutions:

Ajai Choudhry, Jarosław Wróblewski, *Ideal Solutions of the Tarry-Escott Problem of degree eleven with applications to Sums of Thirteenth Powers*, Hardy-Ramanujan Journal, Vol. 31 (2008) pp. 1-13

Solution code: **10.12.14770**

Powers: 2, 4, 6, 8, 10.

Number of terms: **12**

Number of left terms: **6**

Number of right terms: **6**

Left terms:

14770, 12638, 11632, 7115, 7043, 929

Right terms:

14693, 13165, 10112, 9718, 4054, 3455

Remarks:

3rd smallest solution of the infinite family of solutions constructed in:

Ajai Choudhry, Jarosław Wróblewski, *Ideal Solutions of the Tarry-Escott Problem of degree eleven with applications to Sums of Thirteenth Powers*, Hardy-Ramanujan Journal, Vol. 31 (2008) pp. 1-13

Solution code: **10.12.23742**

Powers: 2, 4, 6, 8, 10.

Number of terms: **12**

Number of left terms: **6**

Number of right terms: **6**

Left terms:

23742, 18687, 18372, 12734, 9611, 349

Right terms:

23708, 19653, 16426, 14714, 7713, 3309

Remarks:

4th smallest solution of the infinite family of solutions constructed in:

Ajai Choudhry, Jarosław Wróblewski, *Ideal Solutions of the Tarry-Escott Problem of degree eleven with applications to Sums of Thirteenth Powers*, Hardy-Ramanujan Journal, Vol. 31 (2008) pp. 1-13

Solution code: **10.14.68**

Powers: 2, 4, 6, 8, 10.

Number of terms: **14**

Number of left terms: **7**

Number of right terms: **7**

Left terms:

68, 61, 55, 32, 31, 28, 1

Right terms:

67, 64, 49, 44, 23, 20, 17

Solution code: **10.14.400**

Powers: 2, 4, 6, 8, 10.

Number of terms: **14**

Number of left terms: **7**

Number of right terms: **7**

Left terms:

400, 365, 359, 254, 242, 89, 35

Right terms:

395, 383, 341, 271, 230, 70, 64

Remarks:

Constructed by Tito Piezas and Jarosław Wróblewski (November 2009).

Solution code: **10.14.4139**

Powers: 2, 4, 6, 8, 10.

Number of terms: 14

Number of left terms: 7

Number of right terms: 7

Left terms:

4139, 3812, 3691, 2545, 2468, 979, 448

Right terms:

4111, 3923, 3580, 2684, 2357, 896, 587

Remarks:

Constructed by Tito Piezas and Jarosław Wróblewski (November 2009).

Solution code: **10.14.12689**

Powers: 2, 4, 6, 8, 10.

Number of terms: **14**

Number of left terms: **7**

Number of right terms: **7**

Left terms:

12689, 10560, 9236, 6755, 5745, 3767, 1324

Right terms:

12676, 10711, 8733, 7585, 5280, 3164, 2305

Remarks:

Constructed by Tito Piezas and Jarosław Wróblewski (November 2009).

Solution code: **10.16.93**

Powers: 2, 4, 6, 8, 10.

Number of terms: **16**

Number of left terms: **8**

Number of right terms: **8**

Left terms:

93, 87, 72, 52, 44, 41, 29, 1

Right terms:

92, 89, 67, 61, 39, 36, 33, 8

Solution code: **10.16.113**

Powers: 2, 4, 6, 8, 10.

Number of terms: **16**

Number of left terms: **8**

Number of right terms: **8**

Left terms:

113, 103, 91, 64, 59, 34, 10, 2

Right terms:

112, 106, 85, 74, 53, 26, 23, 1

Solution code: **10.16.132**

Powers: 2, 4, 6, 8, 10.

Number of terms: **16**

Number of left terms: **8**

Number of right terms: **8**

Left terms:

132, 117, 103, 71, 61, 59, 56, 12

Right terms:

131, 121, 92, 84, 72, 43, 39, 37

Solution code: **10.16.155**

Powers: 2, 4, 6, 8, 10.

Number of terms: **16**

Number of left terms: **8**

Number of right terms: **8**

Left terms:

155, 135, 133, 97, 93, 93, 55, 17

Right terms:

153, 145, 115, 107, 105, 83, 43, 33

Solution code: **10.16.172**

Powers: 2, 4, 6, 8, 10.

Number of terms: **16**

Number of left terms: **8**

Number of right terms: **8**

Left terms:

172, 159, 149, 135, 106, 78, 43, 14

Right terms:

169, 166, 140, 138, 111, 74, 37, 27

Solution code: **10.16.173**

Powers: 2, 4, 6, 8, 10.

Number of terms: **16**

Number of left terms: **8**

Number of right terms: **8**

Left terms:

173, 156, 143, 104, 92, 91, 39, 13

Right terms:

168, 167, 123, 116, 113, 61, 44, 29

Solution code: **10.16.188**

Powers: 2, 4, 6, 8, 10.

Number of terms: **16**

Number of left terms: **8**

Number of right terms: **8**

Left terms:

188, 168, 166, 125, 114, 83, 39, 25

Right terms:

183, 182, 151, 131, 120, 62, 60, 19

Solution code: **10.16.193**

Powers: 2, 4, 6, 8, 10.

Number of terms: **16**

Number of left terms: **8**

Number of right terms: **8**

Left terms:

193, 179, 164, 100, 75, 72, 51, 31

Right terms:

191, 184, 159, 109, 68, 60, 53, 45

Remarks:

By a proper sign changes we can make the solution work for powers 1 and 3:

Left terms:

193, -179, 164, -100, 75, 72, 51, -31

Right terms:

191, -184, 159, 109, -68, -60, 53, 45

Solution code: **10.16.2567**

Powers: 2, 4, 6, 8, 10.

Number of terms: **16**

Number of left terms: **8**

Number of right terms: **8**

Left terms:

2567, 2339, 2283, 1544, 1426, 710, 479, 237

Right terms:

2536, 2449, 2173, 1654, 1347, 631, 510, 347

Remarks:

Constructed by Tito Piezas and Jarosław Wróblewski (November 2009).

Solution code: **11.20.107**

Powers: 1, 3, 5, 7, 9, 11.

Number of terms: **20**

Number of left terms: **10**

Number of right terms: **10**

Left terms:

107, 101, 86, 78, 66, 55, 43, 25, 19, 13

Right terms:

106, 103, 81, 79, 73, 50, 38, 30, 27, 6

Remarks:

Derived from solution **10.16.93**.

Solution code: **11.20.139**

Powers: 1, 3, 5, 7, 9, 11.

Number of terms: **20**

Number of left terms: **11**

Number of right terms: **9**

Left terms:

139, 125, 125, 113, 95, 85, 67, 65, 31, 5, 1

Right terms:

137, 133, 119, 107, 101, 91, 61, 53, 49

Remarks:

Derived from solution **10.14.68**.

Solution code: **11.20.178**

Powers: 1, 3, 5, 7, 9, 11.

Number of terms: **20**

Number of left terms: **11**

Number of right terms: **9**

Left terms:

178, 167, 154, 119, 94, 88, 67, 49, 20, 8, 5

Right terms:

175, 173, 148, 124, 100, 74, 62, 59, 34

Remarks:

Derived from solution **10.12.151**.

Solution code: **11.20.199**

Powers: 1, 3, 5, 7, 9, 11.

Number of terms: **20**

Number of left terms: **11**

Number of right terms: **9**

Left terms:

199, 182, 169, 141, 118, 97, 90, 39, 35, 18, 3

Right terms:

194, 193, 149, 147, 139, 78, 70, 66, 55

Remarks:

Derived from solution **10.16.173**.

Solution code: **11.20.327**

Powers: 1, 3, 5, 7, 9, 11.

Number of terms: **20**

Number of left terms: **10**

Number of right terms: **10**

Left terms:

327, 305, 279, 271, 217, 197, 163, 69, 69, 45

Right terms:

321, 317, 277, 255, 229, 213, 119, 97, 95, 19

Remarks:

Derived from solution **10.12.151**.

Solution code: **11.20.329**

Powers: 1, 3, 5, 7, 9, 11.

Number of terms: **20**

Number of left terms: **10**

Number of right terms: **10**

Left terms:

329, 307, 281, 265, 199, 161, 149, 71, 67, 43

Right terms:

323, 319, 275, 253, 227, 145, 121, 97, 95, 17

Remarks:

Derived from solution **10.12.151**.

Solution code: **11.20.431**

Powers: 1, 3, 5, 7, 9, 11.

Number of terms: **20**

Number of left terms: **10**

Number of right terms: **10**

Left terms:

431, 409, 383, 301, 251, 167, 163, 113, 85, 7

Right terms:

425, 421, 371, 317, 223, 199, 151, 125, 43, 35

Remarks:

Derived from solution **10.12.151**.

Solution code: **11.20.569**

Powers: 1, 3, 5, 7, 9, 11.

Number of terms: **20**

Number of left terms: **10**

Number of right terms: **10**

Left terms:

569, 547, 521, 439, 389, 311, 223, 145, 95, 29

Right terms:

563, 559, 509, 455, 361, 337, 197, 173, 79, 35

Remarks:

Derived from solution **10.12.151**.

Solution code: **11.20.3615**

Powers: 1, 3, 5, 7, 9, 11.

Number of terms: **20**

Number of left terms: **10**

Number of right terms: **10**

Left terms:

3615, 2869, 2743, 2427, 1993, 1837, 1767, 1313, 379, 233

Right terms:

3613, 2953, 2499, 2429, 2365, 1683, 1557, 1419, 651, 7

Remarks:

Derived from solution **10.12.1511**.

Solution code: **11.20.5155**

Powers: 1, 3, 5, 7, 9, 11.

Number of terms: **20**

Number of left terms: **9**

Number of right terms: **11**

Left terms:

5155, 4409, 4283, 3533, 3377, 2347, 1919, 887, 733

Right terms:

5153, 4493, 4039, 3905, 2959, 2719, 1547, 1307, 361, 143, 17

Remarks:

Derived from solution **10.12.1511**.

Solution code: **11.20.6269**

Powers: 1, 3, 5, 7, 9, 11.

Number of terms: **20**

Number of left terms: **10**

Number of right terms: **10**

Left terms:

6269, 5945, 5389, 4371, 3935, 2667, 1921, 1741, 435, 371

Right terms:

6227, 6047, 5181, 4741, 3431, 3097, 1963, 1209, 1083, 65

Remarks:

Derived from solution **10.12.2058**.

Solution code: **11.20.6625**

Powers: 1, 3, 5, 7, 9, 11.

Number of terms: **20**

Number of left terms: **11**

Number of right terms: **9**

Left terms:

6625, 6301, 5745, 4727, 4291, 3023, 1995, 1385, 519, 291, 79

Right terms:

6583, 6403, 5537, 5097, 3787, 3453, 1607, 1283, 1231

Remarks:

Derived from solution **10.12.2058**.

Solution code: **11.20.43107**

Powers: 1, 3, 5, 7, 9, 11.

Number of terms: **20**

Number of left terms: **9**

Number of right terms: **11**

Left terms:

43107, 38843, 36831, 27797, 27653, 15819, 15425, 12763, 5869

Right terms:

42953, 39897, 33791, 33003, 21675, 20477, 15973, 9697, 5459, 663, 519

Remarks:

Derived from solution **10.12.14770**.

Solution code: **11.20.48287**

Powers: 1, 3, 5, 7, 9, 11.

Number of terms: **20**

Number of left terms: **11**

Number of right terms: **9**

Left terms:

48287, 44023, 42011, 32977, 32833, 20605, 16889, 7583, 4661, 1477, 689

Right terms:

48133, 45077, 38971, 38183, 26855, 25657, 11837, 10793, 6529

Remarks:

Derived from solution **10.12.14770**.

Solution code: **11.20.65507**

Powers: 1, 3, 5, 7, 9, 11.

Number of terms: **20**

Number of left terms: **9**

Number of right terms: **11**

Left terms:

65507, 55397, 54767, 43491, 37245, 29393, 21283, 17325, 14829

Right terms:

65439, 57329, 50875, 47451, 33449, 29461, 24641, 19351, 7445, 2597, 1199

Remarks:

Derived from solution **10.12.23742**.

Solution code: **11.20.78905**

Powers: 1, 3, 5, 7, 9, 11.

Number of terms: **20**

Number of left terms: **10**

Number of right terms: **10**

Left terms:

78905, 68795, 68165, 56889, 50643, 32119, 30723, 12199, 7885, 1431

Right terms:

78837, 70727, 64273, 60849, 46847, 38039, 24803, 16063, 5323, 1993

Remarks:

Derived from solution **10.12.23742**.

Solution code: **11.22.65**

Powers: 1, 3, 5, 7, 9, 11.

Number of terms: **22**

Number of left terms: **11**

Number of right terms: **11**

Left terms:

65, 60, 59, 47, 45, 40, 30, 18, 16, 10, 4

Right terms:

64, 63, 56, 49, 43, 42, 27, 21, 14, 13, 2

Pure product of:

1, 2, 3, 4, 5, 7, 9, 11, 13, 16, 17, 19, 23.

Solution code: **12.28.81**

Powers: 2, 4, 6, 8, 10, 12.

Number of terms: **28**

Number of left terms: **14**

Number of right terms: **14**

Left terms:

81, 74, 73, 72, 59, 52, 50, 48, 44, 30, 23, 15, 14, 1

Right terms:

80, 78, 71, 69, 62, 54, 49, 47, 40, 33, 25, 18, 4, 4

Pure product of:

1, 3, 4, 5, 6, 7, 10, 11, 13, 16, 17, 19, 23, 27.

Solution code: **12.28.82**

Powers: 2, 4, 6, 8, 10, 12.

Number of terms: **28**

Number of left terms: **14**

Number of right terms: **14**

Left terms:

82, 75, 74, 73, 60, 51, 49, 47, 33, 24, 21, 15, 12, 6

Right terms:

81, 79, 72, 70, 63, 54, 45, 44, 36, 27, 18, 17, 9, 5

Pure product of:

1, 3, 4, 5, 6, 7, 10, 11, 13, 16, 17, 19, 23, 29.

Solution code: **12.28.169**

Powers: 2, 4, 6, 8, 10, 12.

Number of terms: **28**

Number of left terms: **14**

Number of right terms: **14**

Left terms:

169, 151, 149, 145, 105, 101, 99, 95, 71, 63, 51, 47, 43, 23

Right terms:

167, 161, 139, 135, 133, 89, 85, 83, 81, 79, 61, 39, 33, 25

Pure product of:

1, 4, 5, 6, 7, 8, 9, 11, 13, 15, 17, 19, 23, 31.

Solution code: **13.26.173**

Powers: 1, 3, 5, 7, 9, 11, 13.

Number of terms: **26**

Number of left terms: **13**

Number of right terms: **13**

Left terms:

173, 159, 157, 131, 129, 107, 103, 79, 75, 51, 25, 9, 1

Right terms:

171, 167, 141, 139, 137, 97, 93, 89, 85, 43, 19, 15, 3

Pure product of:

1, 3, 4, 5, 6, 7, 9, 10, 11, 13, 16, 17, 19, 23, 29.

Remarks:

Published by L.J. Lander (1973), *Mathematics of Computation* 27 (122), 1973, p. 397

Solution code: **13.28.191**

Powers: 1, 3, 5, 7, 9, 11, 13.

Number of terms: **28**

Number of left terms: **14**

Number of right terms: **14**

Left terms:

191, 177, 175, 173, 147, 131, 129, 125, 113, 69, 57, 51, 27, 7

Right terms:

189, 185, 171, 167, 153, 137, 123, 119, 115, 71, 67, 37, 21, 17

Pure product of:

1, 3, 4, 5, 6, 7, 10, 11, 13, 16, 17, 19, 23, 27, 29.

Solution code: **13.30.69**

Powers: 1, 3, 5, 7, 9, 11, 13.

Number of terms: **30**

Number of left terms: **14**

Number of right terms: **16**

Left terms:

69, 64, 62, 61, 50, 48, 41, 40, 38, 27, 19, 16, 15, 15

Right terms:

68, 67, 60, 59, 54, 46, 45, 34, 32, 31, 31, 10, 9, 8, 6, 5

Pure product of:

1, 2, 3, 4, 5, 6, 7, 9, 10, 11, 13, 15, 16, 17, 19.

Solution code: **13.30.129**

Powers: 1, 3, 5, 7, 9, 11, 13.

Number of terms: **30**

Number of left terms: **13**

Number of right terms: **17**

Left terms:

129, 119, 115, 89, 87, 85, 83, 47, 43, 41, 37, 25, 23

Right terms:

127, 125, 103, 101, 95, 81, 63, 59, 51, 49, 19, 17, 9, 9, 7, 5, 3

Pure product of:

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 13, 14, 17, 19.

Solution code: **14.30.153**

Powers: 2, 4, 6, 8, 10, 12, 14.

Number of terms: **30**

Number of left terms: **15**

Number of right terms: **15**

Left terms:

153, 143, 139, 115, 111, 111, 103, 89, 61, 59, 57, 53, 47, 5, 3

Right terms:

151, 149, 127, 123, 123, 99, 95, 93, 73, 65, 51, 43, 41, 23, 1

Pure product of:

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 13, 15, 17, 19, 23.

Solution code: **14.32.187**

Powers: 2, 4, 6, 8, 10, 12, 14.

Number of terms: **32**

Number of left terms: **16**

Number of right terms: **16**

Left terms:

187, 173, 171, 157, 127, 125, 123, 121, 83, 79, 75, 71, 39, 23, 15, 1

Right terms:

185, 181, 159, 155, 151, 115, 111, 107, 103, 99, 61, 57, 37, 33, 17, 13

Pure product of:

1, 3, 4, 5, 6, 7, 9, 10, 11, 13, 14, 16, 17, 19, 23, 29.

Solution code: **15.34.189**

Powers: 1, 3, 5, 7, 9, 11, 13, 15.

Number of terms: **34**

Number of left terms: **18**

Number of right terms: **16**

Left terms:

189, 179, 175, 173, 159, 149, 129, 127, 97, 85, 55, 41, 31, 25, 17, 11, 3, 1

Right terms:

187, 185, 171, 169, 161, 155, 121, 119, 117, 69, 63, 39, 37, 21, 19, 13

Pure product of:

1, 2, 3, 4, 5, 6, 7, 9, 10, 11, 13, 14, 16, 17, 19, 23, 29.

Solution code: **16.42.95**

Powers: 2, 4, 6, 8, 10, 12, 14, 16.

Number of terms: **42**

Number of left terms: **21**

Number of right terms: **21**

Left terms:

95, 90, 88, 77, 75, 71, 70, 59, 49, 46, 45, 37, 34, 28, 17, 16, 16, 13, 13, 12, 9

Right terms:

94, 93, 82, 81, 79, 68, 67, 56, 55, 53, 35, 32, 31, 29, 27, 26, 20, 7, 6, 5, 0

Pure product of:

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 13, 14, 16, 17, 19, 22, 23.

Solution code: **17.48.337**

Powers: 1, 3, 5, 7, 9, 11, 13, 15, 17.

Number of terms: **48**

Number of left terms: **24**

Number of right terms: **24**

Left terms:

337, 329, 315, 287, 287, 285, 273, 245, 243, 221, 219, 189, 179, 153, 123, 119, 95, 93, 87, 85, 45, 31, 21, 1

Right terms:

335, 333, 305, 303, 291, 269, 267, 261, 239, 225, 205, 201, 173, 157, 117, 113, 107, 103, 83, 73, 47, 39, 9, 7

Pure product of:

1, 2, 3, 5, 7, 8, 9, 10, 11, 12, 13, 17, 19, 23, 29, 31, 41, 43, 53.

Solution code: **18.58.257**

Powers: 2, 4, 6, 8, 10, 12, 14, 16, 18.

Number of terms: **58**

Number of left terms: **29**

Number of right terms: **29**

Left terms:

257, 247, 243, 219, 215, 213, 211, 191, 185, 177, 155, 147, 143, 141, 127, 119, 103, 97, 77, 73, 71, 69, 69, 45, 45, 21, 13, 11, 3

Right terms:

255, 253, 231, 227, 227, 203, 197, 197, 195, 169, 159, 157, 139, 131, 123, 121, 111, 93, 87, 81, 65, 63, 57, 53, 35, 29, 23, 9, 5

Pure product of:

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 13, 15, 17, 19, 21, 23, 25, 27, 31.

Remarks:

My original own search gave 64 terms as the best result.

This solution is taken from *The Prouhet-Tarry-Escott Problem Revisited* by Peter Borwein and Colin Ignalls (1993).

Solution code: **18.64.185**

Powers: 2, 4, 6, 8, 10, 12, 14, 16, 18.

Number of terms: **64**

Number of left terms: **32**

Number of right terms: **32**

Left terms:

185, 181, 174, 160, 160, 159, 153, 139, 138, 135, 118, 114, 111, 96, 86, 84, 76, 64, 63, 62, 59, 42, 39, 37, 35, 32, 25, 17, 13, 12, 7, 3

Right terms:

184, 183, 169, 168, 162, 152, 148, 147, 141, 127, 120, 119, 105, 95, 94, 75, 73, 73, 68, 58, 53, 45, 43, 36, 31, 30, 26, 21, 16, 6, 6, 1

Pure product of:

1, 2, 3, 5, 7, 8, 9, 10, 11, 12, 13, 17, 19, 23, 29, 31, 33, 41, 43, 53.

Solution code: **19.65.143**

Powers: 1, 3, 5, 7, 9, 11, 13, 15, 17, 19.

Number of terms: **65**

Number of left terms: **33**

Number of right terms: **32**

Left terms:

143, 138, 136, 124, 122, 121, 120, 110, 103, 101, 99, 88, 87, 86, 85, 84, 83, 66, 65, 64, 53, 51, 51, 50, 49, 37, 25, 18, 16, 14, 13, 9, 4

Right terms:

142, 141, 130, 128, 128, 116, 114, 113, 109, 95, 94, 93, 93, 91, 81, 80, 76, 75, 61, 59, 58, 57, 56, 45, 43, 34, 24, 22, 20, 19, 10, 8

Pure product of:

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 13, 15, 17, 19, 21, 23, 25, 27, 29, 31.

Remarks:

My original own search gave 74 terms as the best result.

This solution is taken from *The Prouhet-Tarry-Escott Problem Revisited* by Peter Borwein and Colin Ignalls (1993).

Solution code: **19.74.287**

Powers: 1, 3, 5, 7, 9, 11, 13, 15, 17, 19.

Number of terms: **74**

Number of left terms: **37**

Number of right terms: **37**

Left terms:

287, 277, 273, 251, 247, 239, 235, 221, 199, 193, 183, 181, 179, 171, 145, 141, 135, 131, 129, 129, 125, 123, 105, 105, 99, 93, 77, 75, 65, 63, 55, 51, 37, 35, 25, 9, 7

Right terms:

285, 283, 261, 259, 255, 231, 227, 225, 207, 191, 189, 185, 167, 155, 151, 149, 139, 137, 137, 133, 113, 111, 109, 97, 97, 91, 83, 81, 79, 53, 49, 43, 43, 39, 23, 17, 1

Pure product of:

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 13, 14, 16, 17, 19, 22, 23, 25, 31, 41.

Solution code: **20.70.173**

Powers: 2, 4, 6, 8, 10, 12, 14, 16, 18, 20.

Number of terms: **70**

Number of left terms: **35**

Number of right terms: **35**

Left terms:

173, 168, 166, 163, 156, 154, 153, 134, 127, 125, 115, 106, 96, 95, 86, 86, 84, 74, 72, 70, 67, 60, 56, 46, 45, 36, 27, 26, 25, 24, 17, 15, 13, 7, 3

Right terms:

172, 171, 162, 161, 160, 158, 148, 136, 126, 123, 119, 101, 100, 91, 89, 88, 79, 78, 75, 69, 65, 59, 53, 49, 41, 40, 30, 30, 21, 20, 18, 18, 8, 6, 2

Pure product of:

1, 2, 3, 4, 5, 6, 7, 8, 9, 11, 13, 15, 17, 19, 21, 23, 25, 27, 29, 31, 33, 37.

Remarks:

My original own search gave 88 terms as the best result.

This solution is taken from *The Prouhet-Tarry-Escott Problem Revisited* by Peter Borwein and Colin Ignalls (1993).

Solution code: **20.88.129**

Powers: 2, 4, 6, 8, 10, 12, 14, 16, 18, 20.

Number of terms: **88**

Number of left terms: **44**

Number of right terms: **44**

Left terms:

129, 126, 123, 122, 118, 113, 113, 111, 102, 97, 92, 91, 90, 89, 86, 79, 76, 70, 70, 70, 65,
59, 59, 53, 52, 49, 44, 43, 37, 37, 33, 32, 31, 24, 17, 16, 16, 15, 12, 11, 9, 5, 4, 0

Right terms:

128, 128, 121, 121, 119, 117, 112, 108, 101, 99, 95, 93, 87, 84, 84, 82, 80, 73, 67, 66, 62,
61, 60, 60, 47, 46, 45, 41, 40, 39, 34, 34, 25, 23, 20, 19, 14, 14, 13, 13, 7, 2, 1, 1

Pure product of:

1, 1, 2, 3, 4, 5, 5, 6, 7, 8, 9, 10, 11, 13, 14, 15, 17, 19, 23, 25, 29, 31.

Solution code: **21.78.178**

Powers: 1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 21.

Number of terms: **78**

Number of left terms: **39**

Number of right terms: **39**

Left terms:

178, 173, 171, 159, 157, 156, 155, 143, 139, 132, 130, 121, 118, 114, 111, 100, 95, 91, 89, 86, 77, 75, 73, 72, 61, 60, 50, 48, 44, 36, 32, 30, 29, 25, 18, 16, 15, 13, 1

Right terms:

177, 176, 165, 163, 163, 151, 149, 148, 141, 129, 128, 124, 122, 110, 106, 105, 94, 93, 90, 81, 81, 80, 69, 67, 62, 58, 55, 46, 45, 40, 35, 26, 23, 23, 21, 19, 11, 10, 7

Pure product of:

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 13, 15, 17, 19, 21, 23, 25, 27, 29, 31, 33, 37.

Remarks:

My original own search gave 92 terms as the best result.

This solution is taken from *The Prouhet-Tarry-Escott Problem Revisited* by Peter Borwein and Colin Ignalls (1993).

Solution code: **21.92.317**

Powers: 1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 21.

Number of terms: **92**

Number of left terms: **46**

Number of right terms: **46**

Left terms:

317, 311, 307, 303, 285, 285, 275, 265, 261, 255, 243, 241, 241, 203, 199, 199, 189, 189, 175, 165, 157, 153, 147, 133, 119, 113, 109, 107, 97, 83, 77, 73, 71, 67, 67, 49, 43, 35, 31, 29, 25, 25, 19, 11, 1, 1

Right terms:

315, 315, 305, 301, 291, 283, 273, 263, 257, 257, 249, 249, 227, 211, 205, 187, 187, 185, 181, 169, 163, 145, 141, 135, 127, 117, 103, 99, 93, 91, 85, 79, 69, 59, 55, 51, 47, 45, 37, 23, 21, 17, 13, 13, 9, 3

Pure product of:

1, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 13, 14, 15, 17, 19, 23, 25, 27, 29, 31, 37.

Solution code: **22.92.285**

Powers: 2, 4, 6, 8, 10, 12, 14, 16, 18, 20, 22.

Number of terms: **92**

Number of left terms: **46**

Number of right terms: **46**

Left terms:

285, 279, 275, 269, 259, 259, 253, 249, 237, 233, 217, 203, 203, 201, 199, 199, 193, 185, 177, 167, 163, 159, 151, 151, 151, 133, 131, 117, 111, 107, 101, 95, 91, 91, 81, 81, 77, 77, 65, 59, 51, 45, 41, 41, 5, 1

Right terms:

283, 283, 273, 265, 261, 261, 257, 247, 231, 231, 221, 215, 209, 197, 191, 189, 189, 179, 179, 179, 175, 157, 155, 139, 139, 139, 137, 115, 109, 105, 105, 103, 89, 89, 83, 79, 73, 73, 67, 63, 61, 39, 33, 31, 21, 19

Pure product of:

1, 1, 2, 3, 4, 5, 6, 7, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 19, 22, 23, 29, 31.

Solution code: **23.94.216**

Powers: 1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 21, 23.

Number of terms: **94**

Number of left terms: **47**

Number of right terms: **47**

Left terms:

216, 211, 209, 197, 195, 194, 193, 180, 177, 173, 168, 166, 152, 151, 149, 145, 138, 133, 126, 121, 113, 109, 102, 101, 99, 87, 82, 77, 70, 66, 65, 62, 54, 53, 51, 48, 39, 38, 37, 34, 26, 23, 15, 14, 12, 10, 3

Right terms:

215, 214, 203, 201, 201, 189, 187, 186, 176, 175, 167, 162, 158, 153, 143, 142, 139, 136, 128, 118, 114, 111, 103, 100, 92, 89, 86, 75, 72, 69, 64, 61, 57, 47, 47, 45, 45, 41, 33, 33, 29, 25, 21, 13, 9, 8, 2

Pure product of:

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 13, 15, 17, 19, 21, 23, 25, 27, 29, 31, 33, 35, 37, 41.

Remarks:

My original own search gave 118 terms as the best result.

This solution is taken from *The Prouhet-Tarry-Escott Problem Revisited* by Peter Borwein and Colin Ignalls (1993).

Solution code: **23.118.279**

Powers: 1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 21, 23.

Number of terms: **118**

Number of left terms: **61**

Number of right terms: **57**

Left terms:

279, 273, 273, 273, 259, 253, 251, 247, 245, 235, 221, 221, 205, 197, 197, 195, 187, 177, 171, 169, 165, 157, 147, 137, 135, 135, 129, 129, 123, 123, 121, 117, 117, 95, 89, 87, 81, 79, 79, 73, 73, 73, 73, 71, 67, 65, 61, 47, 41, 31, 25, 23, 23, 23, 19, 15, 13, 13, 11, 5, 3

Right terms:

277, 277, 275, 267, 261, 255, 249, 249, 243, 233, 227, 213, 209, 201, 199, 193, 181, 175, 175, 163, 161, 161, 153, 151, 133, 133, 127, 125, 125, 119, 113, 113, 105, 103, 99, 93, 93, 91, 77, 77, 75, 75, 63, 57, 51, 51, 45, 45, 45, 43, 39, 39, 37, 27, 27, 27, 1

Pure product of:

1, 1, 2, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23.

Solution code: **24.114.471**

Powers: 2, 4, 6, 8, 10, 12, 14, 16, 18, 20, 22, 24.

Number of terms: **114**

Number of left terms: **57**

Number of right terms: **57**

Left terms:

471, 461, 457, 433, 429, 427, 425, 399, 385, 375, 371, 367, 363, 343, 341, 339, 337, 335, 333, 329, 313, 305, 291, 285, 281, 277, 257, 247, 243, 241, 233, 197, 193, 171, 169, 147, 145, 145, 141, 139, 117, 113, 111, 107, 99, 83, 75, 59, 55, 51, 51, 45, 27, 27, 23, 21, 3

Right terms:

469, 467, 445, 441, 441, 417, 413, 411, 383, 379, 373, 355, 355, 351, 349, 347, 345, 325, 323, 321, 317, 307, 297, 293, 275, 263, 261, 259, 251, 227, 223, 211, 187, 177, 165, 159, 153, 133, 129, 129, 125, 121, 105, 101, 97, 93, 81, 65, 57, 57, 39, 37, 33, 29, 15, 9, 7

Pure product of:

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 13, 15, 17, 19, 21, 23, 25, 27, 29, 31, 33, 35, 37, 39, 41.

Remarks:

My original own search gave 136 terms as the best result.

This solution is taken from *The Prouhet-Tarry-Escott Problem Revisited* by Peter Borwein and Colin Ignalls (1993).

Solution code: **24.136.385**

Powers: 2, 4, 6, 8, 10, 12, 14, 16, 18, 20, 22, 24.

Number of terms: **136**

Number of left terms: **68**

Number of right terms: **68**

Left terms:

385, 375, 371, 349, 343, 337, 333, 331, 329, 321, 307, 303, 295, 293, 287, 281, 273, 267, 267, 265, 261, 251, 239, 231, 225, 223, 213, 209, 207, 201, 197, 197, 195, 185, 159, 159, 145, 143, 139, 137, 131, 131, 129, 127, 123, 121, 117, 115, 115, 103, 89, 73, 73, 67, 61, 61, 59, 51, 51, 49, 47, 45, 39, 37, 33, 19, 9, 3

Right terms:

383, 381, 361, 355, 347, 345, 327, 325, 319, 313, 313, 311, 305, 297, 291, 275, 271, 269, 259, 255, 249, 247, 243, 241, 237, 233, 229, 219, 193, 189, 183, 183, 177, 177, 173, 167, 163, 161, 151, 147, 147, 135, 113, 111, 111, 107, 107, 101, 99, 97, 91, 85, 83, 81, 77, 71, 69, 65, 65, 43, 41, 29, 27, 21, 15, 11, 1, 1

Pure product of:

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 19, 20, 22, 23, 25, 26, 29, 31, 37.

Solution code: **25.138.483**

Powers: 1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 21, 23, 25.

Number of terms: **138**

Number of left terms: **68**

Number of right terms: **70**

Left terms:

483, 473, 469, 455, 441, 439, 437, 433, 429, 411, 405, 401, 399, 397, 383, 379, 375, 371, 353, 349, 347, 345, 343, 343, 341, 339, 313, 311, 303, 297, 295, 289, 285, 281, 259, 255, 253, 251, 249, 247, 215, 211, 209, 205, 183, 175, 157, 153, 153, 151, 147, 125, 123, 121, 119, 117, 111, 89, 85, 81, 67, 63, 57, 53, 45, 35, 25, 17

Right terms:

481, 479, 459, 453, 453, 449, 425, 423, 421, 417, 415, 413, 395, 391, 385, 373, 367, 363, 363, 359, 359, 357, 331, 329, 329, 327, 323, 321, 319, 301, 287, 279, 275, 273, 273, 271, 265, 235, 235, 231, 229, 223, 221, 189, 185, 177, 171, 145, 141, 137, 135, 133, 133, 133, 127, 105, 105, 101, 99, 77, 69, 51, 49, 47, 43, 41, 19, 15, 11, 5

Pure product of:

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 15, 17, 19, 21, 23, 25, 27, 29, 31, 33, 35, 37, 39, 41.

Remarks:

My original own search gave 150 terms as the best result.

This solution is taken from *The Prouhet-Tarry-Escott Problem Revisited* by Peter Borwein and Colin Ignalls (1993).

Solution code: **25.150.187.186.185**

Powers: 1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 21, 23, 25.

Number of terms: **150**

Number of left terms: **72**

Number of right terms: **78**

Left terms:

187, 184, 183, 182, 173, 170, 167, 162, 160, 160, 159, 154, 150, 149, 149, 145, 143, 140, 140, 136, 130, 127, 127, 126, 126, 123, 121, 121, 116, 116, 110, 108, 106, 105, 103, 102, 101, 101, 94, 93, 93, 88, 88, 83, 81, 77, 73, 71, 68, 66, 66, 64, 61, 60, 60, 59, 44, 42, 33, 31, 29, 28, 27, 27, 27, 25, 22, 22, 20, 20, 7, 3

Right terms:

186, 185, 185, 178, 175, 172, 166, 163, 158, 157, 156, 155, 153, 152, 152, 144, 142, 141, 135, 134, 133, 131, 128, 124, 122, 120, 119, 119, 119, 118, 114, 112, 111, 109, 100, 98, 97, 95, 92, 91, 90, 89, 87, 85, 84, 79, 78, 76, 75, 75, 58, 56, 54, 52, 52, 51, 46, 46, 45, 45, 43, 41, 21, 18, 17, 15, 13, 13, 12, 11, 10, 8, 8, 6, 6, 5, 2, 1

Pure product of:

1, 2, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 21, 23, 25, 26, 27, 29, 31.

Solution code: **25.150.187.186.186**

Powers: 1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 21, 23, 25.

Number of terms: **150**

Number of left terms: **74**

Number of right terms: **76**

Left terms:

187, 184, 182, 180, 174, 171, 167, 163, 163, 161, 159, 154, 150, 150, 150, 150, 146, 143, 141, 139, 133, 131, 129, 129, 126, 126, 122, 122, 120, 116, 113, 109, 108, 106, 103, 101, 101, 88, 88, 73, 71, 69, 68, 67, 67, 65, 60, 60, 53, 48, 47, 45, 43, 39, 36, 34, 32, 32, 32, 30, 30, 28, 27, 27, 25, 24, 23, 19, 15, 4, 4, 4, 2, 2

Right terms:

186, 186, 181, 179, 175, 172, 166, 165, 162, 158, 158, 155, 153, 151, 151, 149, 145, 144, 138, 138, 134, 132, 132, 128, 125, 123, 123, 119, 119, 117, 115, 114, 112, 104, 102, 99, 95, 91, 84, 79, 75, 72, 72, 70, 59, 59, 55, 52, 52, 51, 49, 46, 44, 42, 38, 38, 38, 35, 33, 31, 31, 31, 29, 18, 17, 17, 16, 14, 13, 10, 9, 5, 5, 3, 1, 1

Pure product of:

1, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 22, 23, 25, 26, 27, 29, 31.

Solution code: **26.160.397**

Powers: 2, 4, 6, 8, 10, 12, 14, 16, 18, 20, 22, 24, 26.

Number of terms: **160**

Number of left terms: **80**

Number of right terms: **80**

Left terms:

397, 391, 387, 383, 371, 365, 353, 349, 345, 343, 335, 325, 325, 315, 311, 305, 305, 297, 295, 291, 277, 269, 267, 267, 259, 251, 249, 249, 249, 241, 241, 233, 229, 219, 213, 201, 193, 193, 191, 187, 185, 181, 177, 175, 167, 163, 159, 157, 153, 143, 143, 143, 139, 127, 119, 117, 109, 103, 95, 95, 81, 77, 77, 69, 69, 65, 61, 61, 55, 53, 47, 21, 21, 15, 13, 5, 5, 5, 1, 1

Right terms:

395, 395, 385, 381, 373, 367, 351, 347, 347, 341, 337, 321, 319, 319, 319, 313, 303, 293, 293, 285, 273, 265, 265, 265, 261, 261, 257, 257, 255, 245, 231, 227, 209, 207, 207, 203, 203, 199, 199, 199, 195, 189, 179, 169, 155, 149, 149, 149, 145, 145, 145, 145, 141, 141, 141, 115, 97, 93, 91, 91, 91, 87, 83, 83, 73, 71, 51, 39, 37, 37, 33, 31, 29, 25, 25, 25, 23, 17, 17, 3

Pure product of:

1, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 25, 26, 34, 35.

Solution code: **27.174.204**

Powers: 1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 21, 23, 25, 27.

Number of terms: **174**

Number of left terms: **88**

Number of right terms: **86**

Left terms:

204, 201, 198, 197, 191, 191, 188, 184, 184, 182, 178, 169, 166, 166, 165, 163, 163, 150, 148, 148, 146, 145, 144, 144, 141, 131, 131, 128, 126, 126, 125, 125, 122, 122, 112, 112, 109, 105, 105, 105, 102, 99, 99, 92, 91, 90, 87, 84, 84, 84, 81, 79, 77, 77, 75, 69, 64, 64, 62, 59, 59, 58, 56, 52, 49, 46, 46, 44, 43, 43, 41, 40, 38, 34, 28, 26, 26, 25, 24, 23, 20, 16, 8, 6, 5, 5, 3, 2

Right terms:

203, 203, 196, 196, 194, 190, 189, 186, 183, 177, 176, 174, 172, 168, 162, 156, 155, 155, 154, 153, 149, 142, 139, 137, 136, 136, 136, 134, 133, 121, 121, 121, 117, 117, 115, 114, 114, 113, 104, 101, 100, 100, 96, 94, 93, 89, 89, 86, 83, 80, 80, 76, 76, 74, 74, 72, 70, 68, 67, 57, 54, 54, 54, 53, 50, 48, 48, 47, 45, 39, 36, 35, 35, 33, 33, 31, 30, 27, 27, 15, 15, 15, 14, 13, 7, 1

Pure product of:

1, 1, 2, 3, 4, 5, 5, 6, 7, 8, 9, 10, 11, 11, 12, 13, 14, 15, 16, 17, 19, 21, 23, 25, 26, 27, 29, 31, 37.

Solution code: **28.196.449**

Powers: 2, 4, 6, 8, 10, 12, 14, 16, 18, 20, 22, 24, 26, 28.

Number of terms: **196**

Number of left terms: **98**

Number of right terms: **98**

Left terms:

449, 443, 437, 435, 423, 423, 417, 409, 409, 405, 397, 379, 373, 373, 371, 367, 365, 337, 337, 337, 333, 331, 331, 329, 329, 311, 303, 303, 303, 295, 293, 293, 265, 265, 265, 257, 251, 251, 245, 239, 239, 237, 231, 231, 231, 225, 225, 223, 209, 201, 199, 195, 195, 191, 187, 187, 179, 167, 165, 161, 159, 159, 159, 159, 153, 151, 145, 145, 133, 129, 125, 123, 119, 99, 93, 93, 93, 91, 89, 81, 73, 73, 67, 67, 65, 59, 55, 53, 53, 49, 29, 25, 21, 19, 13, 13, 13, 11

Right terms:

447, 447, 433, 433, 429, 421, 419, 413, 407, 395, 393, 389, 385, 377, 361, 355, 353, 353, 349, 341, 335, 327, 327, 319, 315, 315, 313, 313, 309, 289, 283, 283, 275, 275, 255, 255, 249, 249, 247, 247, 241, 241, 241, 229, 221, 219, 219, 213, 211, 211, 207, 203, 189, 183, 183, 181, 177, 177, 175, 169, 163, 157, 155, 149, 149, 149, 143, 141, 141, 135, 127, 113, 113, 113, 101, 95, 87, 83, 77, 77, 75, 71, 71, 71, 71, 69, 63, 45, 43, 41, 35, 35, 31, 9, 9, 7, 5, 1

Pure product of:

1, 1, 2, 3, 4, 5, 5, 6, 7, 8, 9, 10, 11, 11, 12, 13, 14, 15, 16, 17, 19, 21, 23, 25, 26, 27, 29, 31, 37, 41.

Solution code: **29.207.219**

Powers: 1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 21, 23, 25, 27, 29.

Number of terms: **207**

Number of left terms: **98**

Number of right terms: **109**

Left terms:

219, 216, 216, 216, 209, 206, 205, 203, 202, 197, 194, 193, 190, 189, 186, 185, 183, 182, 178, 175, 172, 168, 163, 162, 159, 159, 152, 152, 148, 147, 141, 140, 138, 137, 133, 132, 129, 123, 120, 116, 110, 107, 104, 103, 101, 101, 100, 100, 97, 92, 92, 92, 91, 88, 74, 71, 70, 70, 69, 69, 67, 66, 66, 65, 64, 61, 61, 61, 61, 58, 57, 54, 39, 39, 36, 36, 34, 34, 33, 31, 31, 30, 30, 30, 30, 30, 28, 27, 27, 27, 26, 24, 24, 24, 23, 21, 18, 18

Right terms:

218, 218, 217, 213, 210, 207, 204, 204, 201, 196, 195, 192, 191, 188, 187, 187, 181, 180, 179, 176, 174, 166, 161, 161, 160, 158, 157, 149, 149, 146, 144, 142, 139, 136, 130, 128, 125, 125, 119, 118, 114, 112, 111, 105, 102, 99, 94, 93, 93, 90, 90, 87, 87, 84, 82, 81, 81, 78, 75, 72, 72, 68, 63, 63, 56, 53, 52, 52, 50, 49, 48, 47, 47, 46, 44, 43, 43, 43, 40, 40, 40, 38, 37, 32, 32, 32, 29, 19, 17, 16, 16, 13, 13, 13, 12, 11, 10, 10, 8, 8, 8, 7, 7, 7, 5, 3, 2, 1, 1

Pure product of:

1, 1, 2, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29.

Solution code: **30.228.441**

Powers: 2, 4, 6, 8, 10, 12, 14, 16, 18, 20, 22, 24, 26, 28, 30.

Number of terms: **228**

Number of left terms: **114**

Number of right terms: **114**

Left terms:

441, 435, 435, 433, 433, 431, 421, 413, 405, 399, 397, 389, 389, 381, 381, 373, 373, 371, 371, 359, 359, 357, 349, 345, 339, 329, 329, 327, 321, 319, 313, 311, 307, 307, 299, 297, 295, 289, 285, 285, 283, 269, 269, 267, 257, 249, 247, 247, 235, 235, 233, 223, 221, 219, 209, 205, 203, 195, 187, 187, 187, 185, 185, 171, 161, 159, 151, 143, 143, 141, 141, 141, 141, 133, 133, 125, 125, 125, 123, 123, 117, 101, 93, 91, 85, 81, 81, 77, 77, 73, 71, 71, 71, 63, 63, 63, 63, 61, 61, 55, 55, 39, 31, 23, 21, 13, 13, 11, 11, 11, 3, 1, 1, 1

Right terms:

439, 439, 437, 429, 429, 429, 429, 411, 403, 401, 395, 393, 385, 385, 377, 377, 377, 365, 363, 363, 361, 361, 351, 341, 335, 333, 325, 325, 323, 323, 315, 315, 301, 301, 301, 301, 293, 291, 291, 287, 273, 271, 263, 263, 259, 255, 253, 241, 239, 237, 231, 229, 227, 213, 199, 199, 197, 191, 191, 189, 189, 181, 181, 181, 173, 167, 165, 147, 139, 139, 137, 129, 129, 129, 127, 119, 119, 119, 115, 113, 107, 107, 105, 99, 97, 89, 89, 79, 69, 67, 67, 67, 59, 57, 57, 53, 45, 45, 43, 41, 37, 35, 33, 33, 29, 27, 25, 19, 19, 17, 9, 5, 5

Pure product of:

1, 1, 2, 2, 3, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29.