

Title: Erdős-Hajnal property for dp-minimal graphs

Abstract: A family of graphs \mathcal{F} is said to have *Erdős-Hajnal property* if there is $\tau > 0$ such that for any graph $G \in \mathcal{F}$, there exists an induced subgraph $H \subseteq G$ of size $\geq |G|^\tau$ such that H is a clique (i.e. a graph where every two vertices are adjacent) or H is an anticlique (i.e. a graph where every two vertices are non-adjacent). We show that for each integer $d \geq 2$, the family $\mathcal{F}_d = \{G = (V, E) : G \text{ and } \overline{G} \text{ have no } d\text{-tuple } (a_1, \dots, a_d) \text{ satisfying that there exists } \{b_{ij}\}_{i \neq j, i, j \in \{1, \dots, d\}} \text{ such that for all } i, j \in \{1, \dots, d\}, E(b_{ij}, a_i) \wedge E(b_{ij}, a_j) \wedge \bigwedge_{k \neq i, j} \neg E(b_{ij}, a_k)\}$ has

Erdős-Hajnal property. In particular, if T is a dp-minimal theory, E a definable symmetric binary relation and $\mathcal{M} \models T$ then the family $\{G = (V, E) : V \subseteq M \text{ a finite set and for every two vertices } x, y \in V, E(x, y) \text{ iff } \mathcal{M} \models E(x, y)\}$ has Erdős-Hajnal property .