

Title: Erdős-Hajnal property for dp-minimal graphs

Abstract: A family of graphs  $\mathcal{F}$  is said to have *Erdős-Hajnal property* if there is  $\tau > 0$  such that for any graph  $G \in \mathcal{F}$ , there exists an induced subgraph  $H \subseteq G$  of size  $\geq |G|^\tau$  such that  $H$  is a clique (i.e. a graph where every two vertices are adjacent) or  $H$  is an anticlique (i.e. a graph where every two vertices are non-adjacent). We show that for each integer  $d \geq 2$ , the family  $\mathcal{F}_d = \{G = (V, E) : G$  and  $\overline{G}$  have no  $d$ -tuple  $(a_1, \dots, a_d)$  satisfying that there exists  $\{b_{ij}\}_{i \neq j, i, j \in \{1, \dots, d\}}$  such that for all  $i, j \in \{1, \dots, d\}$ ,  $E(b_{ij}, a_i) \wedge E(b_{ij}, a_j) \wedge \bigwedge_{k \neq i, j} \neg E(b_{ij}, a_k)\}$  has

Erdős-Hajnal property. In particular, if  $T$  is a dp-minimal theory,  $E$  a definable symmetric binary relation and  $\mathcal{M} \models T$  then the family  $\{G = (V, E) : V \subseteq M$  a finite set and for every two vertices  $x, y \in V$ ,  $E(x, y)$  iff  $\mathcal{M} \models E(x, y)\}$  has Erdős-Hajnal property .