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CENTRAL LIMIT THEOREM FOR A GAUSSIAN INCOMPRESSIBLE FLOW WITH ADDITIONAL BROWNIAN NOISE

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Abstract: We generalize the result of Komorowski and Papanicolaou published in [7]. We consider the solution of stochastic differential equation

$$dX(t) = V(t, X(t))dt + \sqrt{2\kappa}dB(t),$$

where B(t) is a standard *d*-dimensional Brownian motion and $V(t, x), (t, x) \in \mathbb{R} \times \mathbb{R}^d$, is a *d*-dimensional, incompressible, stationary, random Gaussian field decorrelating in finite time. We prove that the weak limit as $\epsilon \downarrow 0$ of the family of rescaled processes $X_{\epsilon}(t) = \epsilon X(t/\epsilon^2)$ exists and may be identified as a certain Brownian motion.

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