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BOUNDARY VALUE PROBLEMS FOR THE DUNKL LAPLACIAN

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Abstract: Let Δ_k be the Dunkl Laplacian on \mathbb{R}^d associated with a reflection group W and a multiplicity function k. The purpose of this paper is to establish the existence and the uniqueness of a positive solution on the unit ball B of \mathbb{R}^d to the following boundary value problem:

 $\Delta_k u = \varphi(u)$ in B and u = f on ∂B .

We distinguish two cases of nonnegative perturbation φ : trivial and nontrivial.

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