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FUNCTIONAL LIMIT THEOREMS FOR PROBABILITY MEASURES ON HYPERGROUPS

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Abstract: Let K be a hypergroup with left Haar measure and (ν_n) a sequence of symmetric probability measures on K converging to ϵ_e . We will prove a functional limit theorem in the sense that convergence $\nu_n^{k_n} \to \mu \in \mathcal{M}^1(K)$ implies unique embeddability of μ into a symmetric convolution semigroup $(\mu_t)_{t\geq 0}$ and $\nu_n^{[k_nt]} \to \mu_t$ holds for all t > 0. This generalizes the corresponding result for hermitian hypergroups. Furthermore, by analogy with locally compact groups, it can be shown that for specific hypergroups similar results are available without symmetry assumptions.

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